

STAT 509 2017 Summer Quiz 2 Distributions

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Binomial: $E(Y) = np$ and $\text{var}(Y) = np(1 - p)$.

$$p_Y(y) = \begin{cases} \binom{n}{y} p^y (1-p)^{n-y} & \text{for } y = 0, 1, 2, \dots, n, \\ 0 & \text{otherwise.} \end{cases}$$

Geometric: $E(Y) = \frac{1}{p}$ and $\text{var}(Y) = \frac{1-p}{p^2}$.

$$p_Y(y) = \begin{cases} (1-p)^{y-1} p & y = 1, 2, 3, \dots \\ 0 & \text{otherwise.} \end{cases}$$

Negative Binomial: $E(Y) = \frac{r}{p}$ and $\text{var}(Y) = \frac{r(1-p)}{p^2}$.

$$p_Y(y) = \begin{cases} \binom{y-1}{r-1} p^r (1-p)^{y-r} & y = 1, 2, 3, \dots \\ 0 & \text{otherwise.} \end{cases}$$

Hypergeometric: $E(Y) = n \left(\frac{r}{N} \right)$ and $\text{var}(Y) = n \left(\frac{r}{N} \right) \left(\frac{N-r}{N} \right) \left(\frac{N-n}{N-1} \right)$.

$$p_Y(y) = \begin{cases} \frac{\binom{r}{y} \binom{N-r}{n-y}}{\binom{N}{n}}, & y \leq r \text{ and } n-y \leq N-r \\ 0, & \text{otherwise.} \end{cases}$$

Poisson: $E(Y) = \lambda t$ and $\text{var}(Y) = \lambda t$.

$$p_Y(y) = \begin{cases} \frac{(\lambda t)^y e^{-\lambda t}}{y!}, & y = 0, 1, 2, \dots \\ 0, & \text{otherwise.} \end{cases}$$

Exponential: $E(Y) = \frac{1}{\lambda}$ and $\text{var}(Y) = \frac{1}{\lambda^2}$.

$$\begin{aligned} f_Y(y) &= \lambda e^{-\lambda y}, \quad y \geq 0 \\ F_Y(y) &= 1 - e^{-\lambda y}, \quad y \geq 0. \end{aligned}$$

Weibull: $E(Y) = \delta \Gamma \left(1 + \frac{1}{\beta} \right)$ and $\text{var}(Y) = \delta^2 \left[\Gamma \left(1 + \frac{2}{\beta} \right) - \left(\Gamma \left(1 + \frac{1}{\beta} \right) \right)^2 \right]$.

$$\begin{aligned} f_Y(y) &= \frac{\beta}{\delta} \left(\frac{y}{\delta} \right)^{\beta-1} e^{-(y/\delta)^\beta}, \quad y \geq 0 \\ F_Y(y) &= 1 - e^{-(y/\delta)^\beta}, \quad y \geq 0. \end{aligned}$$